



[Home Page](#)

[Title Page](#)



[Page 1 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

Introduction to limited area modelling

Laura Rontu
laura_rontu@fmi.fi

March 23, 2005



FINNISH METEOROLOGICAL INSTITUTE



[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 2 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

Contents

Limited area model

[Definitions](#)

[Model](#)

[Basic equations](#)

Lateral boundaries

[The problem of boundaries](#)

[Practical solutions](#)

Problems of lower boundary

[Vertical coordinate of HIRLAM](#)

[Fine resolution problems and solutions](#)

Physical parametrizations

[Introduction to parametrizations](#)

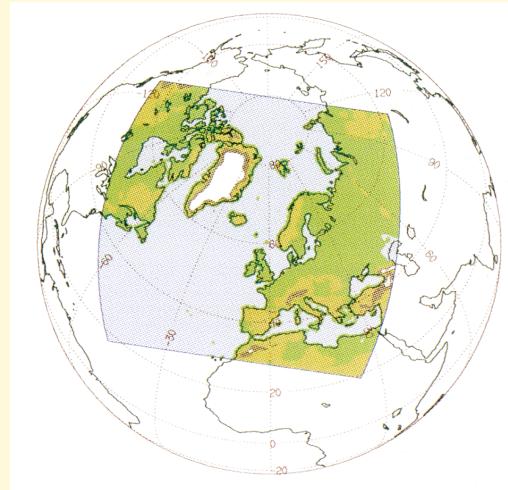
[Parametrization schemes of HIRLAM](#)

[Home Page](#)[Title Page](#)[<<](#)[>>](#)[◀](#)[▶](#)

Page 3 of 13

[Go Back](#)[Full Screen](#)[Close](#)[Quit](#)

Definitions

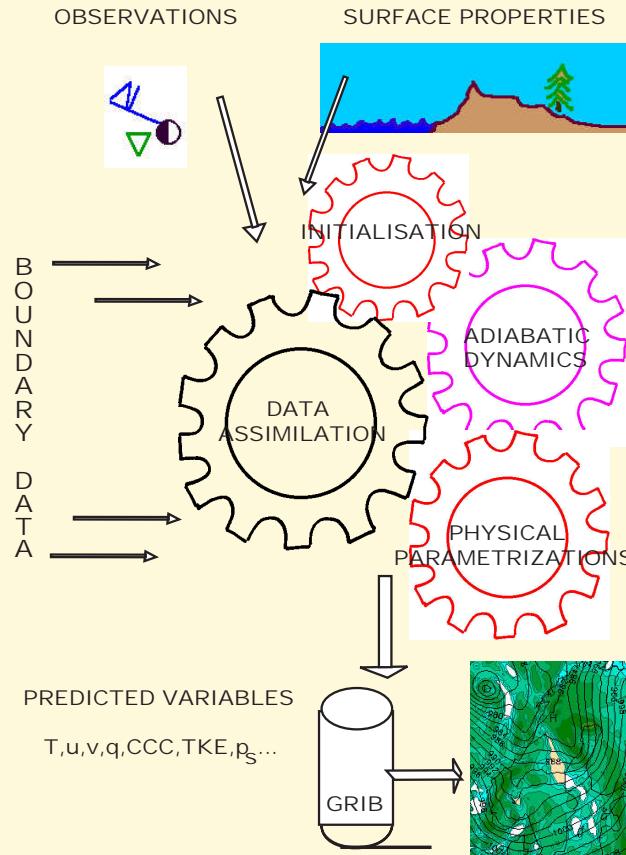


- NWP model = Numerical Weather Prediction model
- LAM = Limited Area Model
- HIRLAM = HIgh Resolution Limited Area Model

Model	Domain	Grid size	Forecast length	Time step
Global	globe/hemisphere	$O(100 \text{ km})$	days - years	$O(30 \text{ min})$
Regional	$O(1000 \text{ km})$	$O(10 \text{ km})$	days - years	$O(10 \text{ min})$
Local	$O(100 \text{ km})$	$O(1 \text{ km})$	day	$O(1 \text{ min})$



Model



[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 4 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)



[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 5 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

Basic equations

$$\frac{du}{dt} + \frac{1}{\rho} \frac{\partial p}{\partial x} + fv = F_x \quad (1)$$

$$\frac{dv}{dt} + \frac{1}{\rho} \frac{\partial p}{\partial y} - fu = F_y \quad (2)$$

$$0 = -\frac{1}{\rho} \frac{\partial p}{\partial z} - g \quad (3)$$

$$c_v \frac{dT}{dt} + p \frac{d\rho^{-1}}{dt} = Q \quad (4)$$

$$\frac{dq}{dt} = S \quad (5)$$

$$\frac{dC}{dt} = P \quad (6)$$

$$\frac{1}{\rho} \frac{d\rho}{dt} = - \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right) \quad (7)$$

$$p = \rho RT \quad (8)$$



[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 6 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

Solving the equations in LAM

- grid, or the coordinate system
- initial state
- lower and upper boundary conditions
- lateral boundary conditions
- resolved and parametrized processes

Grid

Course of Atmospheric Sciences, Hyytiälä 21-26.10.2002 Regional modelling, Laura Rontu 20

[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 7 of 13](#)

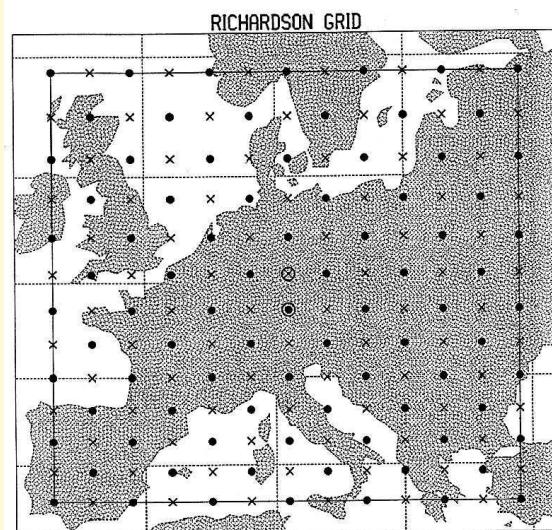
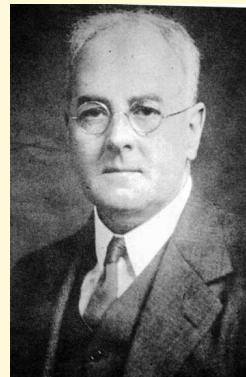
[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

The first numerical forecast



Lewis Fry Richardson, 1881-1953 and his grid, 1922

[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

[Page 8 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

The first numerical forecast calculated with a computer

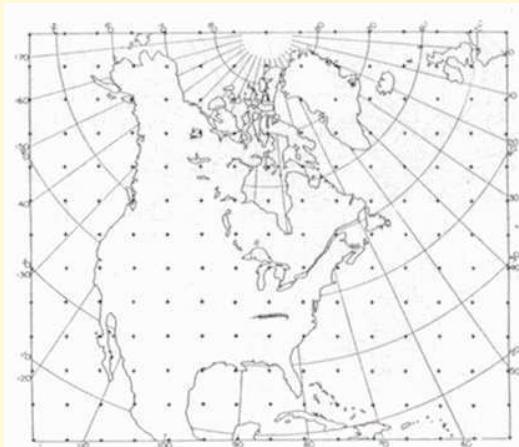


Fig. 1. A typical finite-difference grid used in the computations. A strip two grid intervals in width at the top and side borders and one grid interval in width at the lower border is not shown.

Jule Charney, 1917-1981 and the grid

[Home Page](#)[Title Page](#)[<<](#) [>>](#)[◀](#) [▶](#)

Page 9 of 13

[Go Back](#)[Full Screen](#)[Close](#)[Quit](#)

The problem of lateral boundaries

Transparent/well posed boundaries - difficult

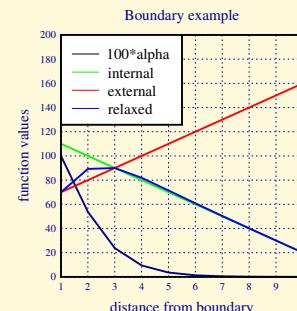
In practice:

Davies relaxation for all prognostic variables within a boundary zone of e.g. 8 grid points wide

$$\phi_i = (1 - \alpha_i)\phi_i^{in} + \alpha_i\phi^{out} \quad (9)$$

where

$$\alpha_i = 1 - \tanh[(i - 1)/2)] \quad (10)$$



Practical boundaries

- fresh and good boundary data
- keep the boundaries as far as possible
- horizontal and vertical interpolation
- filtering of boundaries



Stretched coordinates - an alternative?

[Home Page](#)

[Title Page](#)

[<<](#)

[>>](#)

[◀](#)

[▶](#)

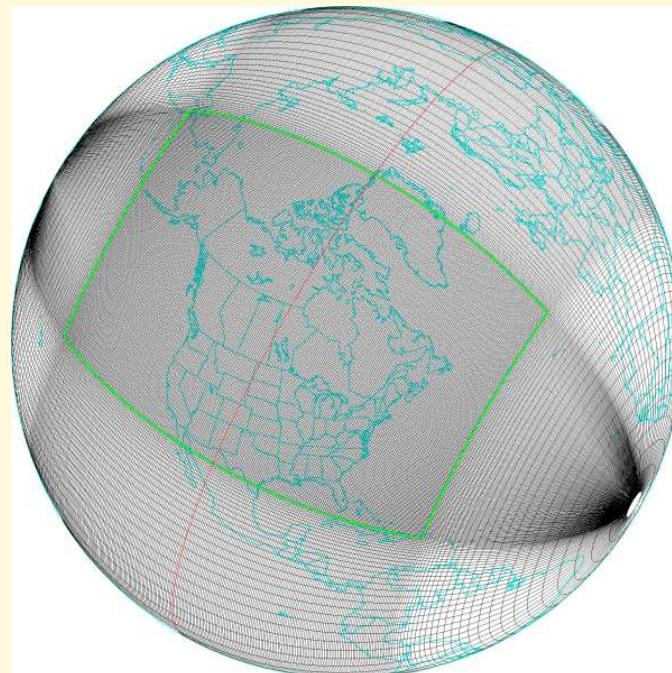
[Page 10 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)



[Home Page](#)[Title Page](#)[<<](#) [>>](#)[◀](#) [▶](#)

Page 11 of 13

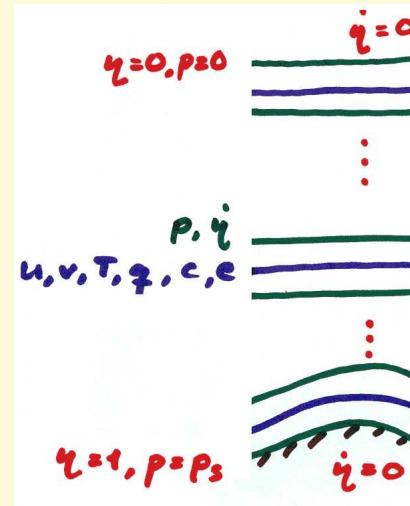
[Go Back](#)[Full Screen](#)[Close](#)[Quit](#)

Lower boundary problems

Vertical coordinate of HIRLAM

Terrain-following hybrid levels: pressure at model level k

$$p_k(x, y) = a_k(z) + b_k(z)p_s(x, y) \quad (11)$$



Fine scale modelling problems related to the lower boundary condition

[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

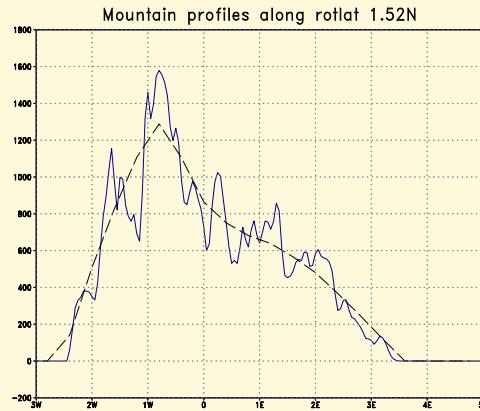
[Page 12 of 13](#)

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)

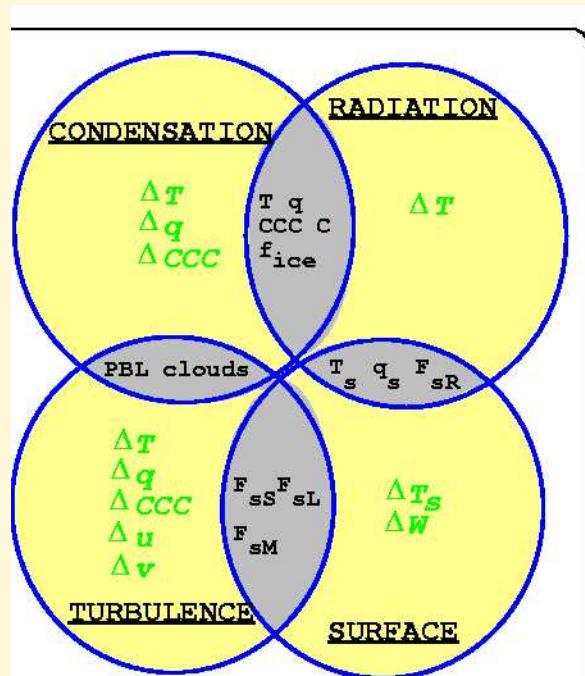


An example of mountains profile accross Southern Scandinavian mountains. Grid-size of HIRLAM 5.5 km (dashed) and 44 km (solid).

- free-slip and no-slip conditions (surface friction)
- practical problems for numerical schemes (semi-Lagrangian) \Rightarrow filtering of orography
- streamlines over orography, flow blocking and turbulence
- smoothing of numerical noise with the 4th order horizontal diffusion

Introduction to physical parametrizations

- Right hand side of the equations = sources and sinks
- Two types of parametrizations: (1) describing very small phenomena and (2) mixing and removing instabilities; Resolved and parametrized processes
- Parametrization provides additional model output variables



Parametrization schemes of HIRLAM

[Home Page](#)

[Title Page](#)

[◀◀](#) [▶▶](#)

[◀](#) [▶](#)

Page 13 of 13

[Go Back](#)

[Full Screen](#)

[Close](#)

[Quit](#)